

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 1

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6xy^2 + yz e^{xyz} + yz e^{xyz} (xyz - 3y), 6x^2y + xz e^{xyz} (xyz - 3y) + (xz - 3) e^{xyz} + 2, xy e^{xyz} + xy e^{xyz} (xyz - 3y))$.
 Compute the potential function for this field whose potential at the origin is -1.
 Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -5.09412 2) 4.50588 3) -1.29412 4) -8.69412

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(8t+2) \sin(2t) (8 \cos(2t) + 8), (4t+7) \sin(t) (8 \cos(2t) + 8)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 9575.15 2) 10851.8 3) 4468.75 4) 6383.65

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{7y, -7y^2, 4yz - 5yz^2\}$ and the surface

$$S \equiv \left(\frac{7+x}{1}\right)^2 + \left(\frac{-4+y}{6}\right)^2 + \left(\frac{-7+z}{1}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 15282.2 2) -8042.48 3) -37801.6 4) -23324.2

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 2

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2, 2x^2y + 3z e^{yz} + z e^{yz} (3yz - 2), 3ye^{yz} + ye^{yz} (3yz - 2))$.
 . Compute the potential function for this field whose potential at the origin is 3.
 . Calculate the value of the potential at the point $p=(-8,5,4)$.

$$\begin{aligned} 1) & -\frac{196977072541}{5} + 58e^{20} \quad 2) & -\frac{309535404293}{5} + 58e^{20} \\ 3) & -\frac{126628115196}{5} + 58e^{20} \quad 4) & 1605 + 58e^{20} \end{aligned}$$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\begin{aligned} r: [0, \pi] & \longrightarrow \mathbb{R}^2 \\ r(t) &= \{(4t+4)\sin(2t), (8\cos(4t)+9), (4t+8)\sin(t)\} \end{aligned}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

- 1) 1761.45 2) 377.652 3) 1132.45 4) 1258.25

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-x^2z + 6yz, -5xy, -6yz^2 - 8xyz^2\}$ and the surface

$$S \equiv \left(\frac{6+x}{1}\right)^2 + \left(\frac{2+y}{5}\right)^2 + \left(\frac{-4+z}{9}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 44787.4 2) -111966. 3) -11196.1 4) 134361.

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 3

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-\sin(xy z) - xyz \cos(xy z) + 1, -x^2 z \cos(xy z), -x^2 y \cos(xy z))$.

- a. Compute the potential function for this field whose potential at the origin is 3.
- b. Calculate the value of the potential at the point $p=(-10,8,0)$.

- 1) -7 2) $-\frac{273}{10}$ 3) $\frac{63}{10}$ 4) $-\frac{231}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} - \frac{\sqrt{3}-1}{2\sqrt{2}} \right) \cos(t) (5 \cos(t)+7)}{\sin^2(t)+1}, \frac{\left(\frac{1+\sqrt{3}}{2\sqrt{2}} - \frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} \right) \cos(t) (5 \cos(t)+7)}{\sin^2(t)+1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 112.46 2) 70.4602 3) 49.4602 4) 77.4602

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{5x - \sin[2y^2 + 2z^2], z - 5yz + \sin[2x^2], 5xyz + \cos[2x^2 + y^2]\}$ and the surface

$$S \equiv \left(\frac{5+x}{6} \right)^2 + \left(\frac{y}{7} \right)^2 + \left(\frac{-6+z}{9} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 35627.4 2) -154381. 3) -39584.1 4) -130630.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 4

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (4xy - 3y \sin(xy) + y(-3xy - 1) \cos(xy) + y^2, 2x^2 + 2xy - 3x \sin(xy) + x(-3xy - 1) \cos(xy), 0)$. Compute the potential function for this field whose potential at the origin is -4.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -18.0536 2) -4.05365 3) 12.4464 4) 9.44635

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(7t+9) \sin(2t), (8 \cos(18t) + 9), (7t+6) \sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 1670.88 2) 7098.38 3) 3340.88 4) 4175.88

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-3z^2 - 2x^2y^2z^2, 5x^2y^2z, 4xy + 7y^2z^2\}$ and the surface

$$S \equiv \left(\frac{3+x}{8}\right)^2 + \left(\frac{8+y}{7}\right)^2 + \left(\frac{4+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -3.14858×10^7 2) 1.85211×10^7 3) -4.25985×10^7 4) 7.03801×10^7

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 5

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = \left(\frac{yz(3xz - 3yz)}{xyz + 1} + 3z \log(xyz + 1), \right.$

$$\left. , \frac{xz(3xz - 3yz)}{xyz + 1} - 3z \log(xyz + 1), \frac{xy(3xz - 3yz)}{xyz + 1} + (3x - 3y) \log(xyz + 1) \right)$$

). Compute the potential function for this field whose potential at the origin is -1.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 2. 2) -1. 3) -3.4 4) -1.9

Exercise 2

Compute the area of the domain whose boundary is the curve

$$r: [0, \pi] \rightarrow \mathbb{R}^2$$

$$r(t) = \{(2t+8) \sin(2t) (8 \cos(6t) + 9), (5t+1) \sin(t) (8 \cos(6t) + 9)\}$$

Indication: it is necessary to represent

the curve to check whether it has intersection points.

- 1) 20079. 2) 13901. 3) 15445.5 4) 16990.

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-5z^2 + 3xy^2z^2, x^2yz - 5y^2z^2, 7z^2 + 6x^2yz^2\}$ and the surface

$$S \equiv \left(\frac{6+x}{9} \right)^2 + \left(\frac{-5+y}{1} \right)^2 + \left(\frac{-5+z}{2} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 4.26864×10^6 2) -2.51096×10^6 3) 1.25548×10^6 4) 2.38541×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 6

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6xy^2 + xyz^2 \sin(xz) - yz \cos(xz) + 2x, 6x^2y - xz \cos(xz), x^2yz \sin(xz) - xy \cos(xz))$. Compute the potential function for this field whose potential at the origin is 2.

. Calculate the value of the potential at the point $p=(6,-4,-5)$.

- 1) $\frac{8773}{2} - 120 \cos[30]$ 2) $\frac{19312}{5} - 120 \cos[30]$ 3) $\frac{29794}{5} - 120 \cos[30]$ 4) $1766 - 120 \cos[30]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (5 \cos(t) + 9) \left(\frac{(1+\sqrt{3}) \cos(t)}{2\sqrt{2}} - \frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} \right), \sin(2t) (5 \cos(t) + 9) \left(\frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} + \frac{(\sqrt{3}-1) \cos(t)}{2\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 73.4347 2) 36.9347 3) 102.635 4) 7.73473

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-5 + 4y + \sin[y^2 + z^2], e^{-x^2-2z^2} + 5y + 4yz, -5xy + 3z - \sin[x^2 - y^2]\}$ and the surface

$$S \equiv \left(\frac{x}{4} \right)^2 + \left(\frac{y}{7} \right)^2 + \left(\frac{-1+z}{8} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 24770.3 2) 28148. 3) 11259.5 4) 38281.1

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 7

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2z^2(yz+1), x^2y^2z^3 + 2x^2yz^2(yz+1) - 4y, x^2y^3z^2 + 2x^2y^2z(yz+1))$

1). Compute the potential function for this field whose potential at the origin is -2.

2). Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -2.6088 2) 9.0912 3) -11.0088 4) -9.8088

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(4t+3)\sin(2t), (8\cos(6t)+9), (5t+8)\sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 324.105 2) 1616.91 3) 2101.71 4) 485.705

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{2 - 9x^2y^2z^2, 7x^2y^2 - 6yz^2, -3xy^2z\}$ and the surface

$$S \equiv \left(\frac{6+x}{5}\right)^2 + \left(\frac{y}{5}\right)^2 + \left(\frac{2+z}{2}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1.80144×10^6 2) -1.53652×10^6 3) 2.01337×10^6 4) 529834.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 8

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (x y (1 - 2 z), z + y z (x - 2 x z) - 2 y^2 - y, -4 x y + x z (x - 2 x z) - x, x y (x - 2 x z) - 2 x^2 y z)$. Compute the potential function for this field whose potential at the origin is -4. Calculate the value of the potential at the point $p=(-2,7,4)$.

- 1) -2601 2) 0 3) -578 4) $\frac{4913}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{1}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right) \cos(t) (4 \cos(t) + 5)}{\sin^2(t) + 1}, \frac{\left(\frac{\sin(t)}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right) \cos(t) (4 \cos(t) + 5)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 38.7345 2) 12.1345 3) 23.5345 4) 19.7345

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{e^{-2y^2+2z^2} - 2y, 6x + \cos[2x^2 - z^2], -3z - \sin[2x^2 - 2y^2]\}$ and the surface

$$S \equiv \left(\frac{-3+x}{9} \right)^2 + \left(\frac{3+y}{5} \right)^2 + \left(\frac{z}{3} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -7635.96 2) 2885.44 3) -1696.46 4) 0.539967

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 9

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (x z^2 \cos(xz) + z \sin(xz) + 2x, 0, x^2 z \cos(xz) + x \sin(xz))$

- . Compute the potential function for this field whose potential at the origin is 2.
- . Calculate the value of the potential at the point $p=(0,-5,10)$.

- 1) $-\frac{4}{5}$ 2) $\frac{18}{5}$ 3) $\frac{29}{5}$ 4) 2

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(-\frac{\sin(t)}{\sqrt{2}} - \frac{1}{\sqrt{2}} \right) \cos(t) (9 \cos(t) + 10)}{\sin^2(t) + 1}, \frac{\left(\frac{1}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right) \cos(t) (9 \cos(t) + 10)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 169.531 2) 152.631 3) 34.331 4) 254.031

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{1 - 4xyz + \sin[y^2 + 2z^2], 3xy + \cos[x^2 + 2z^2], e^{2x^2 - 2y^2} + 3xyz\}$ and the surface

$$S \equiv \left(\frac{-5+x}{1} \right)^2 + \left(\frac{-8+y}{9} \right)^2 + \left(\frac{-9+z}{4} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 9228.94 2) -66908.7 3) -23071.9 4) -41529.5

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 10

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz(3x+y)e^{xyz} + 3e^{xyz} - 3y, xz(3x+y)e^{xyz} + e^{xyz} - 3x, xy(3x+y)e^{xyz})$. Compute the potential function for this field whose potential at the origin is -4.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -5.05152 2) -2.35152 3) 8.14848 4) 9.34848

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(-\frac{\sin(t)}{\sqrt{2}} - \frac{1}{\sqrt{2}} \right) \cos(t) (3 \cos(t) + 9)}{\sin^2(t) + 1}, \frac{\left(\frac{1}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right) \cos(t) (3 \cos(t) + 9)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 123.926 2) 62.3257 3) 18.3257 4) 88.7257

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-9xz + 3yz + \cos[y^2 + 2z^2], e^{2x^2+2z^2} - 3xyz, -8xy + \cos[2x^2 - 2y^2]\}$ and the surface $S \equiv \left(\frac{7+x}{2} \right)^2 + \left(\frac{-4+y}{1} \right)^2 + \left(\frac{-1+z}{8} \right)^2 = 1$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1527.85 2) -2009.75 3) 804.248 4) -2331.35

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 11

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2 \sin(xy z) + yz(2x - 2y) \cos(xy z) - 3y^2 + 3, -2 \sin(xy z) + xz(2x - 2y) \cos(xy z) - 6xy, xy(2x - 2y) \cos(xy z))$.

. Compute the potential function for this field whose potential at the origin is -1.

. Calculate the value of the potential at the point $p=(2,3,-2)$.

$$1) -\frac{541}{10} + 2 \sin[12] \quad 2) -\frac{347}{5} + 2 \sin[12] \quad 3) -49 + 2 \sin[12] \quad 4) -\frac{857}{5} + 2 \sin[12]$$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{1}{2} - \frac{1}{2} \sqrt{3} \sin(t)\right) \cos(t) (3 \cos(t) + 8)}{\sin^2(t) + 1}, \frac{\left(\frac{\sin(t)}{2} + \frac{\sqrt{3}}{2}\right) \cos(t) (3 \cos(t) + 8)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

$$1) 135.626 \quad 2) 121.426 \quad 3) 71.7257 \quad 4) 22.0257$$

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{4xy + 3xz + \cos[2y^2], e^{-2x^2+2z^2} - 11y, -6 - \sin[2x^2 - 2y^2]\}$ and the surface

$$S \equiv \left(\frac{7+x}{1} \right)^2 + \left(\frac{-9+y}{9} \right)^2 + \left(\frac{-4+z}{9} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

$$1) 42681. \quad 2) 17575. \quad 3) 12553.8 \quad 4) 13809.1$$

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 12

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (3x^2y^3(y-z) + 2y^2, x^3y^3 + 3x^3y^2(y-z) + 4xy, -x^3y^3)$. Compute the potential function for this field whose potential at the origin is -4.

. Calculate the value of the potential at the point $p=(-7,6,-7)$.

- 1) -963 652 2) $-\frac{1927\,304}{5}$ 3) $\frac{963\,652}{5}$ 4) $-\frac{9154\,694}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(6t+5)\sin(2t), (8\cos(6t)+8), (2t+8)\sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 462.635 2) 1539.94 3) 770.435 4) 2155.54

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-7 - 4x^2, 6xy - 4yz, -7x^2\}$ and the surface

$$S \equiv \left(\frac{-1+x}{4}\right)^2 + \left(\frac{-2+y}{9}\right)^2 + \left(\frac{9+z}{9}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 87672.4 2) 46143.7 3) 18457.9 4) -9227.89

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 13

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-z(2xyz + 1)\sin(xz) + 2yz\cos(xz) - 2x, 2xz\cos(xz), 2xy\cos(xz) - x(2xyz + 1)\sin(xz))$

-). Compute the potential function for this field whose potential at the origin is 4.
- . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) 3.83264 2) -7.26736 3) 8.93264 4) 0.832636

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(8t+3)\sin(2t), (7\cos(18t)+9), (9t+5)\sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 1498.43 2) 5991.23 3) 375.225 4) 3744.83

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-8yz, 4z^2, -6x^2yz - 9xy^2z\}$ and the surface

$$S \equiv \left(\frac{2+x}{6}\right)^2 + \left(\frac{-1+y}{4}\right)^2 + \left(\frac{7+z}{6}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 5066.76 2) 0.760632 3) -13677.4 4) 13679.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 14

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-3xyz^2 \sin(xy) + 3z \cos(xy)) \mathbf{i} + (6xy - 3x^2z^2 \sin(xy), 3x \cos(xy) - 3x^2yz \sin(xy)) \mathbf{j}$

1). Compute the potential function for this field whose potential at the origin is -5.

2). Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -11.3806 2) 5.81944 3) -3.78056 4) -6.98056

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{\sin(2t)(-\cos(t))(6\cos(t) + 9), -(\sin(t)\sin(2t)(6\cos(t) + 9))\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 77.7544 2) 8.45442 3) 147.054 4) 16.1544

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \left\{ e^{-2y^2-z^2} - xz, e^{-2x^2-2z^2} + 8xz, -2xy + xz - \sin[2x^2+y^2] \right\}$ and the surface

$$S \equiv \left(\frac{-6+x}{1} \right)^2 + \left(\frac{8+y}{4} \right)^2 + \left(\frac{-8+z}{7} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -681.072 2) -422.572 3) -234.572 4) 329.428

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 15

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6xy^2 - yz(1-2xyz)\sin(xy) - 2yz\cos(xy)) - 1, 6x^2y - xz(1-2xyz)\sin(xy) - 2xz\cos(xy), -xy(1-2xyz)\sin(xy) - 2xy\cos(xy)$. Compute the potential function for this field whose potential at the origin is 6.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -7.91961 2) 4.58039 3) -10.4196 4) 5.58039

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{-(\sin(t) \sin(2t) (9 \cos(t) + 9)), \sin(2t) \cos(t) (9 \cos(t) + 9)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 123.926 2) 95.4259 3) 47.9259 4) 152.426

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-8x + \cos[2y^2 - 2z^2], 8xz + \cos[z^2], -3y - \sin[2x^2 - y^2]\}$ and the surface

$$S \equiv \left(\frac{3+x}{6}\right)^2 + \left(\frac{-5+y}{5}\right)^2 + \left(\frac{2+z}{6}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 10254.5 2) -6031.86 3) 13270.5 4) -4825.46

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 16

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (z \cos(yz) - 2, 3 \cos(yz) - z(xz + 3y) \sin(yz), x \cos(yz) - y(xz + 3y) \sin(yz))$

-). Compute the potential function for this field whose potential at the origin is -4.
- . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) 11.4089 2) -3.39106 3) -14.1911 4) -0.591058

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(6t+1) \sin(2t) (9 \cos(20t) + 10), (2t+8) \sin(t) (9 \cos(20t) + 10)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 22311.7 2) 20080.6 3) 17849.5 4) 29005.

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-3y^2 - 3xy^2z, -2xyz + 6xz^2, -8y^2z\}$ and the surface

$$S \equiv \left(\frac{9+x}{9}\right)^2 + \left(\frac{-4+y}{9}\right)^2 + \left(\frac{2+z}{2}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -252081. 2) -68129.8 3) 183951. 4) -20438.8

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 17

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2 + 2z \sin(xy z) + yz(2xz + 2y) \cos(xy z) - y^2, 2x^2y + 2 \sin(xy z) + xz(2xz + 2y) \cos(xy z) - 2xy, 2x \sin(xy z) + xy(2xz + 2y) \cos(xy z))$. Compute the potential function for this field whose potential at the origin is 1.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -0.185156 2) 1.61484 3) 1.21484 4) -0.585156

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ -\frac{\sin(t) \cos(t) (7 \cos(t) + 9)}{\sin^2(t) + 1}, \frac{\cos(t) (7 \cos(t) + 9)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 147.662 2) 221.462 3) 123.062 4) 73.862

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{3yz + \sin[y^2 + 2z^2], 7y + \sin[2x^2 - 2z^2], -6xy + \sin[y^2]\}$ and the surface

$$S \equiv \left(\frac{-1+x}{7}\right)^2 + \left(\frac{-4+y}{9}\right)^2 + \left(\frac{-2+z}{9}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -6649.69 2) 23275.3 3) -13299.7 4) 16625.3

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 18

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-y z (-3 x y - 3) \sin(x y z) - 3 y \cos(x y z) + 2, -x z (-3 x y - 3) \sin(x y z) - 3 x \cos(x y z), -x y (-3 x y - 3) \sin(x y z))$.
). Compute the potential function for this field whose potential at the origin is -1.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -1.66487 2) 2.33513 3) 0.335132 4) -0.664868

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{\sin(2t) \cos(t) (\cos(t) + 1), \sin(t) \sin(2t) (\cos(t) + 1)\}$$

Indication: it is necessary to represent
 the curve to check whether it has intersection points.

- 1) 0.778097 2) 1.5781 3) 1.1781 4) 0.678097

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \left\{ -5 + e^{-y^2} - 9 x y z, e^{-x^2+z^2}, -z - \sin[2 x^2] \right\}$ and the surface

$$S \equiv \left(\frac{-7+x}{9} \right)^2 + \left(\frac{9+y}{7} \right)^2 + \left(\frac{8+z}{5} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 0.674484 2) -1.71267×10^6 3) 1.71267×10^6 4) -856 335.

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 19

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = \left(\frac{yz(2xyz - 3z)}{xyz + 1} + 2yz \log(xyz + 1) - 4xy, \right.$

$$\left. -2x^2 + \frac{xz(2xyz - 3z)}{xyz + 1} + 2xz \log(xyz + 1), \frac{xy(2xyz - 3z)}{xyz + 1} + (2xy - 3) \log(xyz + 1) \right).$$

-). Compute the potential function for this field whose potential at the origin is -1.
- . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 3.31149 2) -1.48851 3) -7.88851 4) -3.68851

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{ (3t + 6) \sin(2t) (3 \cos(19t) + 10), (8t + 5) \sin(t) \}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 2594.86 2) 260.265 3) 4410.66 4) 4151.26

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{ 6y^2 - 5xz^2, -7x^2 - 3x^2yz^2, 6x - 6y^2z \}$ and the surface

$$S \equiv \left(\frac{-6+x}{3} \right)^2 + \left(\frac{-2+y}{7} \right)^2 + \left(\frac{-1+z}{8} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1.67186×10^6 2) -5.01559×10^6 3) -1.19419×10^6 4) -2.50779×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 20

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz e^{xyz} + 6xy, 3x^2 + xz e^{xyz}, xy e^{xyz})$.
 . Compute the potential function for this field whose potential at the origin is 6.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 6.6465 2) -8.3535 3) 24.6465 4) 16.8465

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t)(9\cos(t) + 9) \left(\frac{\cos(t)}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right), \sin(2t)(9\cos(t) + 9) \left(\frac{\sin(t)}{\sqrt{2}} + \frac{\cos(t)}{\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent
 the curve to check whether it has intersection points.

- 1) 114.426 2) 95.4259 3) 28.9259 4) 66.9259

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-12 + e^{-2y^2-2z^2}, -4x - 9xz + \cos[2x^2 - 2z^2], -5xz - \sin[y^2]\}$ and the surface

$$S \equiv \left(\frac{-5+x}{5} \right)^2 + \left(\frac{2+y}{4} \right)^2 + \left(\frac{-7+z}{6} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -33930.3 2) -12566.4 3) -50267.4 4) 18851.1

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 21

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (4xy + y \cos(xy) + 2y, 2x^2 + x \cos(xy) + 2x, 0)$.
 . Compute the potential function for this field whose potential at the origin is 4.
 . Calculate the value of the potential at the point $p=(-6,9,-8)$.

- 1) $-\frac{2992}{5} - \sin[54]$ 2) $-544 - \sin[54]$ 3) $544 - \sin[54]$ 4) $-\sin[54]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(8t+9) \sin(2t), (7 \cos(14t) + 10), (2t+6) \sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 2910.67 2) 1323.07 3) 2646.07 4) 3175.27

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-4y, 2yz, -xy^2z\}$ and the surface

$$S \equiv \left(\frac{2+x}{3}\right)^2 + \left(\frac{-8+y}{7}\right)^2 + \left(\frac{1+z}{3}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 0.93479 2) -38421.1 3) 38422.9 4) -42263.3

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 22

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (z(2x-y)\cos(xz) + 2\sin(xz) + 2x, 6y - \sin(xz), x(2x-y)\cos(xz))$. Compute the potential function for this field whose potential at the origin is -1. Calculate the value of the potential at the point $p=(8,-10,-9)$.

- 1) $363 - 26 \sin[72]$ 2) $-\frac{5127}{5} - 26 \sin[72]$ 3) $\frac{6443}{5} - 26 \sin[72]$ 4) $-\frac{2813}{5} - 26 \sin[72]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(5t+6)\sin(2t)(\cos(8t)+6), (5t+4)\sin(t)(\cos(8t)+6)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 3320.19 2) 8299.59 3) 830.494 4) 5809.89

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-9xy^2z, -x^2y^2, -7x^2yz\}$ and the surface

$$S \equiv \left(\frac{-1+x}{9}\right)^2 + \left(\frac{-9+y}{3}\right)^2 + \left(\frac{-8+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -1.1978×10^7 2) 9.64898×10^6 3) 5.32358×10^6 4) -3.32723×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 23

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2y^2 - 3, 4xy, 0)$

-). Compute the potential function for this field whose potential at the origin is -1.
- . Calculate the value of the potential at the point $p=(-6,0,0)$.

1) $\frac{102}{5}$ 2) 17 3) $\frac{306}{5}$ 4) $\frac{119}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(t+4) \sin(2t) (5 \cos(8t) + 5), (6t+3) \sin(t) (5 \cos(8t) + 5)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

1) 3903.5 2) 3548.7 3) 5677.5 4) 1065.1

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{0, -3x^2z, -2x^2 + 9x^2z\}$ and the surface

$$S \equiv \left(\frac{-7+x}{3}\right)^2 + \left(\frac{2+y}{1}\right)^2 + \left(\frac{-8+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) 82732. 2) 22981.4 3) 32173.8 4) 27577.6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 24

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6x, 0, 0)$

-). Compute the potential function for this field whose potential at the origin is 1.
- . Calculate the value of the potential at the point $p=(6,5,7)$.

1) $\frac{2289}{10}$ 2) $-\frac{327}{10}$ 3) 109 4) $-\frac{1853}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (2\cos(t) + 8) \left(-\frac{\sin(t)}{2} - \frac{1}{2}\sqrt{3}\cos(t) \right), \sin(2t) (2\cos(t) + 8) \left(\frac{\cos(t)}{2} - \frac{1}{2}\sqrt{3}\sin(t) \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

1) 87.5363 2) 77.3363 3) 51.8363 4) 41.6363

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$$\{-9xyz + \sin[y^2 + 2z^2], 2y - \sin[2z^2], 6 + xyz + \cos[2x^2 - 2y^2]\}$$

$$S \equiv \left(\frac{6+x}{2} \right)^2 + \left(\frac{y}{7} \right)^2 + \left(\frac{3+z}{7} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) -1395.7 2) 821.003 3) -246.297 4) 1724.1

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 25

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = \left(4xy^2 + \frac{3yz}{xz+1}, 4x^2y + 3\log(xz+1) - 6y, \frac{3xy}{xz+1}\right)$. Compute the potential function for this field whose potential at the origin is 4. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) -1.26464 2) 3.53536 3) 3.83536 4) -1.86464

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(4t+1)\sin(2t)(6\cos(13t)+6), (t+8)\sin(t)(6\cos(13t)+6)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 8648.07 2) 5595.87 3) 5087.17 4) 6104.57

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{9xz, -xyz^2, 2x^2z^2\}$ and the surface

$$S \equiv \left(\frac{9+x}{6}\right)^2 + \left(\frac{2+y}{6}\right)^2 + \left(\frac{1+z}{5}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 185 661. 2) -232 076. 3) 139 246. 4) -255 283.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 26

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz(2yz+3)\cos(xy) + 3y, 2z\sin(xy) + xz(2yz+3)\cos(xy) + 3x - 1, 2y\sin(xy) + xy(2yz+3)\cos(xy))$.

. Compute the potential function for this field whose potential at the origin is 2.

. Calculate the value of the potential at the point $p=(-5,-10,6)$.

1) $\frac{949}{5} - 117 \sin[300]$ 2) $162 - 117 \sin[300]$ 3) $\frac{254}{5} - 117 \sin[300]$ 4) $\frac{5814}{5} - 117 \sin[300]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(4t+5)\sin(2t), (5\cos(18t)+5), (8t+7)\sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 2859.78 2) 1655.78 3) 1505.28 4) 2257.78

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{x^2 z, 5x - 9yz, 7x^2 z\}$ and the surface

$$S \equiv \left(\frac{6+x}{1}\right)^2 + \left(\frac{-5+y}{5}\right)^2 + \left(\frac{4+z}{3}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 21199.5 2) 12719.9 3) 23319.4 4) 97515.9

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 27

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6x + 2z \log(yz+1),$

$$\frac{z(2xz+y)}{yz+1} + \log(yz+1) - 1, \frac{y(2xz+y)}{yz+1} + 2x \log(yz+1))$$

). Compute the potential function for this field whose potential at the origin is -4.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -3.22741 2) -12.4274 3) 1.57259 4) -12.8274

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(6t+7) \sin(2t) (2 \cos(15t) + 8), (7t+7) \sin(t) (2 \cos(15t) + 8)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 21531.3 2) 32296.5 3) 26913.9 4) 2692.17

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{8xyz^2, -y^2z - 6xyz^2, 8x^2yz + 7xz^2\}$ and the surface

$$S \equiv \left(\frac{-9+x}{7}\right)^2 + \left(\frac{-4+y}{7}\right)^2 + \left(\frac{z}{2}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1.18553×10^6 2) -237105. 3) 3.91224×10^6 4) 4.0308×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 28

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-6xy^2 - 2yz\cos(yz) - 3, -6x^2y - z(2yz - 2xyz)\sin(yz) + (2z - 2xz)\cos(yz), (2y - 2xy)\cos(yz) - y(2yz - 2xyz)\sin(yz))$.

1. Compute the potential function for this field whose potential at the origin is 1.

2. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) 2.88655 2) -0.613447 3) 3.08655 4) 1.28655

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t)(4\cos(t) + 6) \left(\frac{(1+\sqrt{3})\cos(t)}{2\sqrt{2}} - \frac{(\sqrt{3}-1)\sin(t)}{2\sqrt{2}} \right), \sin(2t)(4\cos(t) + 6) \left(\frac{(1+\sqrt{3})\sin(t)}{2\sqrt{2}} + \frac{(\sqrt{3}-1)\cos(t)}{2\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 31.1575 2) 44.7575 3) 20.9575 4) 34.5575

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{7x + 4z + \cos[y^2 - 2z^2], 9xyz + \sin[z^2], e^{2x^2-2y^2} + 2yz\}$ and the surface

$$S \equiv \left(\frac{3+x}{8} \right)^2 + \left(\frac{-7+y}{1} \right)^2 + \left(\frac{-3+z}{2} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 10055.8 2) -4021.24 3) 10860.2 4) 3620.56

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 29

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (4xy^2 + yz^2 e^{xz} - 4x, 4x^2y + z e^{xz}, y e^{xz} + xyz e^{xz})$. Compute the potential function for this field whose potential at the origin is -3. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) -3.0853 2) -2.2853 3) -15.8853 4) -6.6853

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(4t+8) \sin(2t) (8 \cos(13t) + 8), (2t+7) \sin(t) (8 \cos(13t) + 8)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 31936.5 2) 18786.3 3) 24422.1 4) 3757.54

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-7xy^2 + 3xz^2, 3yz^2, -9z^2\}$ and the surface

$$S \equiv \left(\frac{-5+x}{2}\right)^2 + \left(\frac{3+y}{8}\right)^2 + \left(\frac{2+z}{2}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -9415.02 2) -11768.8 3) -49429.6 4) -22360.9

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 30

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (6x + (3y - 3yz)\sin(yz), (3x - 3xz)\sin(yz) + z(3xy - 3xyz)\cos(yz), y(3xy - 3xyz)\cos(yz) - 3xy\sin(yz))$.
). Compute the potential function for this field whose potential at the origin is 5.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 12.6809 2) 6.08088 3) 7.28088 4) 11.4809

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t)(4\cos(t) + 7) \left(-\frac{\sin(t)}{\sqrt{2}} - \frac{\cos(t)}{\sqrt{2}} \right), \sin(2t)(4\cos(t) + 7) \left(\frac{\cos(t)}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent
 the curve to check whether it has intersection points.

- 1) 44.7677 2) 13.9677 3) 66.7677 4) 35.9677

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-6 + 8xy + \sin[y^2 - z^2], e^{-2x^2} + 2z, 3xy + \sin[2y^2]\}$ and the surface
 $S \equiv \left(\frac{-4+x}{8} \right)^2 + \left(\frac{2+y}{9} \right)^2 + \left(\frac{-3+z}{1} \right)^2 = 1$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -5790.69 2) -10134.1 3) -4825.49 4) -9168.89

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 31

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-2xy - 2,$

$$-x^2 + \frac{z(-2yz - 3z)}{yz+1} - 2z \log(yz+1), \frac{y(-2yz - 3z)}{yz+1} + (-2y - 3) \log(yz+1)$$

). Compute the potential function for this field whose potential at the origin is 2.

. Calculate the value of the potential at the point $p=(6,1,5).$

- 1) $-46 - 25 \log[6]$ 2) $\frac{359}{10} - 25 \log[6]$ 3) $-\frac{1413}{5} - 25 \log[6]$ 4) $-\frac{2371}{10} - 25 \log[6]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(3t+4) \sin(2t) (8 \cos(20t) + 10), (8t+5) \sin(t) (8 \cos(20t) + 10)\}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

- 1) 13987.2 2) 16784.6 3) 27974.2 4) 36366.4

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-9x^2 + 9x^2y^2, 9y, 5x^2y\}$ and the surface

$$S \equiv \left(\frac{5+x}{3}\right)^2 + \left(\frac{-4+y}{6}\right)^2 + \left(\frac{2+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F}.$

Indication: Use Stoke's Theorem if it is necessary.

- 1) -1.85959×10^6 2) $-599868.$ 3) -2.15953×10^6 4) -59986.2

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 32

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (3 \cos(xy z) - yz(3x+2z) \sin(xy z), -xz(3x+2z) \sin(xy z), 2\cos(xy z) - xy(3x+2z) \sin(xy z))$.
 . Compute the potential function for this field whose potential at the origin is -3.
 . Calculate the value of the potential at the point $p=(0,4,-5)$.

1) $-\frac{117}{10}$ 2) $-\frac{91}{2}$ 3) -13 4) $-\frac{533}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$r: [0, \pi] \rightarrow \mathbb{R}^2$
 $r(t) = \{(8t+3) \sin(2t), (7 \cos(7t) + 8), (5t+4) \sin(t)\}$

Indication: it is necessary to represent
 the curve to check whether it has intersection points.

1) 2254.8 2) 1127.8 3) 902.403 4) 1353.2

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-2x^2yz, -x^2y^2z, 6xz\}$ and the surface

$$S \equiv \left(\frac{-3+x}{5}\right)^2 + \left(\frac{-4+y}{4}\right)^2 + \left(\frac{7+z}{7}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) 2.73617×10^6 2) 2.33575×10^6 3) 667358. 4) 600622.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 33

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-yz(-3xz - 2x)\sin(xy z) + (-3z - 2)\cos(xy z) - 6xy - 4x, -3x^2 - xz(-3xz - 2x)\sin(xy z), -xy(-3xz - 2x)\sin(xy z) - 3x\cos(xy z))$. Compute the potential function for this field whose potential at the origin is 2.

. Calculate the value of the potential at the point $p=(-7,10,-2)$.

- 1) $-\frac{3147}{5} - 28 \cos[140]$ 2) $-\frac{29684}{5} - 28 \cos[140]$
 3) $-7810 - 28 \cos[140]$ 4) $-1566 - 28 \cos[140]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{1}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}} \right) \cos(t) (6 \cos(t) + 7)}{\sin^2(t) + 1}, \frac{\left(\frac{\sin(t)}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right) \cos(t) (6 \cos(t) + 7)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 111.503 2) 79.9027 3) 64.1027 4) 72.0027

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{6y + \cos[y^2], -2 + e^{-2z^2} + 5z, e^{-y^2} + yz\}$ and the surface

$$S \equiv \left(\frac{4+x}{6} \right)^2 + \left(\frac{2+y}{4} \right)^2 + \left(\frac{-8+z}{1} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -79.8619 2) -766.662 3) -201.062 4) -1009.06

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 34

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$$\frac{2xy^2z}{xyz+1} + 2y \log(xyz+1) + 4xy, \frac{2x^2yz}{xyz+1} + 2x^2 + 2x \log(xyz+1), \frac{2x^2y^2}{xyz+1}$$

). Compute the potential function for this field whose potential at the origin is -7.

. Calculate the value of the potential at the point $p=(5,9,10)$.

$$1) 443 + 90 \log[451] \quad 2) -\frac{2093}{2} + 90 \log[451] \quad 3) \frac{21311}{10} + 90 \log[451] \quad 4) -\frac{34297}{10} + 90 \log[451]$$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(7t+8) \sin(2t) (\cos(2t) + 10), (2t+5) \sin(t) (\cos(2t) + 10)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

$$1) 35547.7 \quad 2) 13096.9 \quad 3) 22451.4 \quad 4) 18709.6$$

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-9xy^2z, -9x^2 + 4x^2z, 5x^2y^2z^2\}$ and the surface

$$S \equiv \left(\frac{-6+x}{6}\right)^2 + \left(\frac{-8+y}{1}\right)^2 + \left(\frac{3+z}{8}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

$$1) 4.74962 \times 10^7 \quad 2) 8.189 \times 10^6 \quad 3) -4.42206 \times 10^7 \quad 4) -1.6378 \times 10^7$$

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 35

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-2z \cos(xz) - 3y^2, -6xy, -2x \cos(xz))$.
). Compute the potential function for this field whose potential at the origin is 2.
 . Calculate the value of the potential at the point $p=(8, -8, 7)$.

1) $\frac{16858}{5} - 2 \sin[56]$ 2) $3065 - 2 \sin[56]$ 3) $-1534 - 2 \sin[56]$ 4) $-\frac{10741}{10} - 2 \sin[56]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$r: [0, \pi] \rightarrow \mathbb{R}^2$
 $r(t) = \{(4t+3) \sin(2t), (9 \cos(2t) + 9), (5t+6) \sin(t)\}$

Indication: it is necessary to represent
 the curve to check whether it has intersection points.

1) 2014.74 2) 1209.14 3) 604.942 4) 403.542

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{2x^2y^2z, -6yz, 4xy^2z\}$ and the surface

$$S \equiv \left(\frac{6+x}{3}\right)^2 + \left(\frac{4+y}{1}\right)^2 + \left(\frac{-1+z}{1}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) -9847.01 2) 19697. 3) -6892.61 4) 21666.6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 36

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (y e^{xy} (2x - xyz) + e^{xy} (2 - yz) + 2y, xz (-e^{xy}) + x e^{xy} (2x - xyz) + 2x + 6y, xy (-e^{xy}))$. Compute the potential function for this field whose potential at the origin is -3.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -2.26363 2) -0.263626 3) 1.33637 4) 3.03637

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (3 \cos(t) + 5) \left(-\frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} - \frac{(1+\sqrt{3}) \cos(t)}{2\sqrt{2}} \right), \sin(2t) (3 \cos(t) + 5) \left(\frac{(\sqrt{3}-1) \cos(t)}{2\sqrt{2}} - \frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 36.9692 2) 20.8692 3) 16.2692 4) 23.1692

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$\{-5y + \cos[2y^2 + 2z^2], -8xy + \cos[x^2 + 2z^2], -7 + e^{-2x^2} - 9xyz\}$ and the surface

$$S \equiv \left(\frac{-1+x}{8} \right)^2 + \left(\frac{4+y}{8} \right)^2 + \left(\frac{-5+z}{2} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 45036.6 2) -9006.58 3) -34527. 4) 15012.6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 37

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (1-y(-z-3)z \sin(xyz), -x(-z-3)z \sin(xyz) - 2y, -xy(-z-3) \sin(xyz) - \cos(xyz))$

1). Compute the potential function for this field whose potential at the origin is -6.

2). Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 9.83485 2) -28.6652 3) 11.2348 4) -6.26515

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(2t+1) \sin(2t) (7 \cos(20t) + 10), (9t+6) \sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 465.175 2) 1161.77 3) 1626.17 4) 2090.57

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-x^2y^2, 6z^2, -3z - x^2y^2z^2\}$ and the surface

$$S \equiv \left(\frac{8+x}{6}\right)^2 + \left(\frac{8+y}{3}\right)^2 + \left(\frac{8+z}{8}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1.9241×10^8 2) -5.95555×10^7 3) -6.87179×10^7 4) 4.58119×10^7

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 38

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2 + y(3y - 3z)\cos(xy) + 6xy, 2x^2y + 3x^2 + x(3y - 3z)\cos(xy) + 3\sin(xy), -3\sin(xy))$.
). Compute the potential function for this field whose potential at the origin is -2.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -7.27302 2) 5.72698 3) -1.27302 4) -2.27302

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(2t + 9)\sin(2t)(4\cos(15t) + 7), (6t + 3)\sin(t)(4\cos(15t) + 7)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 11686.6 2) 21035.4 3) 14023.8 4) 12855.2

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{5x^2z - 7x^2y^2z, 2x^2 - 8x^2y, -y + 5x^2z^2\}$ and the surface

$$S \equiv \left(\frac{-8+x}{2}\right)^2 + \left(\frac{8+y}{8}\right)^2 + \left(\frac{z}{1}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 86860.5 2) -52115.5 3) -34743.5 4) -138976.

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 39

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (y(-\sin(yz)) - y, x(-\sin(yz)) + z(-xy - 3z)\cos(yz) - x, y(-xy - 3z)\cos(yz) - 3\sin(yz))$.
 . Compute the potential function for this field whose potential at the origin is -3.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -1.00485 2) 10.5951 3) -0.204852 4) -3.80485

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2 \\ \mathbf{r}(t) = \{ (t+4) \sin(2t) (9 \cos(6t) + 9), (6t+5) \sin(t) \}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 866.214 2) 1559.01 3) 779.614 4) 1472.41

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-7x^2y^2z, -2x - 8x^2y^2, -8x^2y - 5xy^2z^2\}$ and the surface

$$S \equiv \left(\frac{-5+x}{5} \right)^2 + \left(\frac{8+y}{4} \right)^2 + \left(\frac{-1+z}{8} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -849 286. 2) -283 095. 3) -2.83095×10^6 4) 7.36048×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 40

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-4xy^2 + yz^2 - 2, xz^2 - 4x^2y, 2xyz)$

-). Compute the potential function for this field whose potential at the origin is 1.
- . Calculate the value of the potential at the point $p=(-10,8,-9)$.

- 1) $-\frac{558511}{10}$ 2) $-\frac{346662}{5}$ 3) $\frac{211849}{5}$ 4) -19259

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(9t+5) \sin(2t) (3 \cos(4t) + 5), (2t+5) \sin(t) (3 \cos(4t) + 5)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 2024.29 2) 6745.79 3) 2698.79 4) 1349.79

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-6 + x^2y, -8y^2z, -2xy^2 - 2z\}$ and the surface

$$S \equiv \left(\frac{-8+x}{5}\right)^2 + \left(\frac{7+y}{3}\right)^2 + \left(\frac{8+z}{6}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -1.10421×10^6 2) -380761 3) -1.37074×10^6 4) 837677 .

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 41

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-yz(xz + 2yz)\sin(xy) + z\cos(xy)) - 2xy,$
 $-x^2 - xz(xz + 2yz)\sin(xy) + 2z\cos(xy) - 6y, (x + 2y)\cos(xy) - xy(xz + 2yz)\sin(xy)$
). Compute the potential function for this field whose potential at the origin is -4.
. Calculate the integral of the potential function ϕ over the domain $[0,1]^3.$

- 1) 7.55277 2) 7.05277 3) 14.0528 4) -4.44723

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2 \\ \mathbf{r}(t) = \{(t+6)\sin(2t)(9\cos(4t)+9), (3t+5)\sin(t)(9\cos(4t)+9)\}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

- 1) 1332.48 2) 11987.7 3) 14651.5 4) 13319.6

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-8yz + 3xz^2, -7xy, -6z^2\}$ and the surface

$$S \equiv \left(\frac{8+x}{5}\right)^2 + \left(\frac{-3+y}{9}\right)^2 + \left(\frac{-9+z}{1}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}.$

Indication: Use Stoke's Theorem if it is necessary.

- 1) -97509.8 2) -46948.8 3) 36115.7 4) -50560.3

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 42

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (4xy^2 + (3-3z)\sin(xy z), yz(3x-3xz)\cos(xy z) - 2xy, 4x^2y - x^2 + xz(3x-3xz)\cos(xy z), xy(3x-3xz)\cos(xy z) - 3x\sin(xy z))$. Compute the potential function for this field whose potential at the origin is 0. Calculate the value of the potential at the point $p=(2,-9,-10)$.

1) $684 + 66 \sin[180]$ 2) $-\frac{525}{2} + 66 \sin[180]$ 3) $\frac{27663}{10} + 66 \sin[180]$ 4) $\frac{7206}{5} + 66 \sin[180]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [\theta, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{1}{\sqrt{2}} - \frac{\sin(t)}{\sqrt{2}}\right) \cos(t) (6 \cos(t) + 6)}{\sin^2(t) + 1}, \frac{\left(\frac{\sin(t)}{\sqrt{2}} + \frac{1}{\sqrt{2}}\right) \cos(t) (6 \cos(t) + 6)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

1) 33.9027 2) 47.1027 3) 66.9027 4) 93.3027

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{xz + \sin[y^2 + 2z^2], -9z - \sin[2x^2 + 2z^2], e^{y^2} - 2y + 6xyz\}$ and the surface

$$S \equiv \left(\frac{4+x}{4}\right)^2 + \left(\frac{6+y}{8}\right)^2 + \left(\frac{8+z}{8}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) -72917.1 2) 627096. 3) 320840. 4) 145837.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 43

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2y^2 z, 2xyz + z(2xy - 3) + 1, y(2xy - 3))$.
 . Compute the potential function for this field whose potential at the origin is -2.
 . Calculate the value of the potential at the point $p=(5,-7,-7)$.

- 1) $-\frac{32274}{5}$ 2) $-\frac{50204}{5}$ 3) -3586 4) $-\frac{12551}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(7t+2)\sin(2t), (\cos(15t)+7), (7t+3)\sin(t)\}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

- 1) 2359.63 2) 1815.13 3) 544.627 4) 1996.63

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{2y^2 z, -3z + 5xz, -9xy^2 + 8z\}$ and the surface

$$S \equiv \left(\frac{3+x}{2}\right)^2 + \left(\frac{7+y}{9}\right)^2 + \left(\frac{8+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1689.14 2) 6754.34 3) 4342.34 4) 2412.74

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 44

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (3z \sin(yz) - 3, z(3xz + y) \cos(yz) + \sin(yz) - 2y, 3x \sin(yz) + y(3xz + y) \cos(yz))$.
 . Compute the potential function for this field whose potential at the origin is 0.
 . Calculate the value of the potential at the point $p=(-3,1,1)$.

- 1) $\frac{33}{5} - 8 \sin[1]$ 2) $8 - 8 \sin[1]$ 3) $\frac{32}{5} - 8 \sin[1]$ 4) $\frac{49}{10} - 8 \sin[1]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(6t+9) \sin(2t) (4 \cos(7t) + 9), (9t+5) \sin(t) (4 \cos(7t) + 9)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 56180.1 2) 30251.1 3) 73466.1 4) 43215.6

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{2x^2 y^2 z - 7xyz^2, z + 2y^2 z^2, 4x\}$ and the surface

$$S \equiv \left(\frac{7+x}{8}\right)^2 + \left(\frac{1+y}{5}\right)^2 + \left(\frac{1+z}{4}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -72623.1 2) 121039. 3) -48415.3 4) -254182.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 45

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (x^2 y^3 z^3 + 2xy^2 z^2 (xyz - 3) + 6xy^2 + y, x^3 y^2 z^3 + 2x^2 yz^2 (xyz - 3) + 6x^2 y + x, x^3 y^3 z^2 + 2x^2 y^2 z (xyz - 3))$.
) . Compute the potential function for this field whose potential at the origin is 2.
 . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 8.88785 2) 2.08785 3) 2.48785 4) 7.28785

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2 \\ \mathbf{r}(t) = \{\sin(2t) \cos(t) (9 \cos(t) + 10), \sin(t) \sin(2t) (9 \cos(t) + 10)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 22.3484 2) 110.348 3) 11.3484 4) 165.348

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-2y + 5yz + \cos[2y^2], 6y + 2yz + \cos[x^2 + 2z^2], -8xy + \sin[x^2 + 2y^2]\}$ and the surface $S \equiv \left(\frac{-7+x}{8}\right)^2 + \left(\frac{y}{2}\right)^2 + \left(\frac{-2+z}{7}\right)^2 = 1$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 4691.45 2) 15949.8 3) 3753.25 4) 19702.6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 46

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz e^{xz} + 3y^2 + 1, 6xy + e^{xz}, xy e^{xz})$

). Compute the potential function for this field whose potential at the origin is 0.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) 1.15895 2) 0.158951 3) 1.65895 4) 2.45895

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} - \frac{1+\sqrt{3}}{2\sqrt{2}} \right) \cos(t) (8 \cos(t)+8)}{\sin^2(t)+1}, \frac{\left(\frac{\sqrt{3}-1}{2\sqrt{2}} - \frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} \right) \cos(t) (8 \cos(t)+8)}{\sin^2(t)+1} \right\}$$

Indication: it is necessary to represent

the curve to check whether it has intersection points.

- 1) 83.5381 2) 189.738 3) 213.338 4) 118.938

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$\{-7y + 4yz + \cos[2y^2], 6xy - \sin[x^2 - 2z^2], -2 + \cos[2x^2 + 2y^2]\}$ and the surface

$$S \equiv \left(\frac{-1+x}{8} \right)^2 + \left(\frac{-5+y}{5} \right)^2 + \left(\frac{-2+z}{6} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 6031.86 2) 10856.7 3) 3016.36 4) -3014.64

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 47

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (0, 4y, 0)$

-). Compute the potential function for this field whose potential at the origin is -4.
- . Calculate the value of the potential at the point $p=(7, -8, 2)$.

1) $\frac{1984}{5}$ 2) $-\frac{682}{5}$ 3) 124 4) $-\frac{806}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(9t+5) \sin(2t), (6 \cos(10t) + 6), (3t+1) \sin(t)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

1) 353.208 2) 441.508 3) 706.408 4) 883.008

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{7y^2 z, 8 - 9x^2 y^2 z^2, -3x^2\}$ and the surface

$$S \equiv \left(\frac{1+x}{5}\right)^2 + \left(\frac{5+y}{6}\right)^2 + \left(\frac{6+z}{2}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) -6.45908×10^6 2) 4.96853×10^6 3) -5.46538×10^6 4) 1.58993×10^7

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 48

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (y^3 z^4, 3y^2 z^3 (xz - 1) + 4y - 1, xy^3 z^3 + 3y^3 z^2 (xz - 1))$. Compute the potential function for this field whose potential at the origin is 1.

. Calculate the value of the potential at the point $p=(3,2,4)$.

- 1) $\frac{28195}{2}$ 2) $-\frac{5639}{10}$ 3) 5639 4) $\frac{95863}{5}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{1+\sqrt{3}}{2\sqrt{2}} - \frac{(\sqrt{3}-1)\sin(t)}{2\sqrt{2}} \right) \cos(t) (9\cos(t)+10)}{\sin^2(t)+1}, \frac{\left(\frac{(1+\sqrt{3})\sin(t)}{2\sqrt{2}} + \frac{\sqrt{3}-1}{2\sqrt{2}} \right) \cos(t) (9\cos(t)+10)}{\sin^2(t)+1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 304.731 2) 169.531 3) 203.331 4) 287.831

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{e^{-2z^2} + 3yz, -7xy - 5xz - \sin[2x^2 + z^2], 8y + \sin[2x^2 + y^2]\}$ and the surface

$$S \equiv \left(\frac{1+x}{7} \right)^2 + \left(\frac{-8+y}{2} \right)^2 + \left(\frac{1+z}{3} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -122.596 2) 1231.5 3) 3078. 4) 4185.9

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 49

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2 - yz(xyz + x)\sin(xyz) + (yz + 1)\cos(xyz) - 2y^2, 2x^2y - xz(xyz + x)\sin(xyz) + xz\cos(xyz) - 4xy, xy\cos(xyz) - xy(xyz + x)\sin(xyz))$. Compute the potential function for this field whose potential at the origin is 3.

. Calculate the value of the potential at the point $p=(-9,-6,-4)$.

- 1) $3567 - 225 \cos[216]$ 2) $16615 - 225 \cos[216]$
 3) $14751 - 225 \cos[216]$ 4) $-\frac{2669}{5} - 225 \cos[216]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t)(\cos(t) + 6) \left(-\frac{(1+\sqrt{3})\sin(t)}{2\sqrt{2}} - \frac{(\sqrt{3}-1)\cos(t)}{2\sqrt{2}} \right), \sin(2t)(\cos(t) + 6) \left(\frac{(1+\sqrt{3})\cos(t)}{2\sqrt{2}} - \frac{(\sqrt{3}-1)}{2\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 51.067 2) 9.06703 3) 17.467 4) 28.667

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-2 + e^{-y^2+2z^2}, 8xy - 7xyz + \cos[2x^2], -xyz + \cos[2x^2]\}$ and the surface

$$S \equiv \left(\frac{-9+x}{7} \right)^2 + \left(\frac{8+y}{9} \right)^2 + \left(\frac{-2+z}{7} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -3324.38 2) 33250.6 3) 149626. 4) 133001.

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 50

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (2xy^2z^2(-xy - 3y) - x^2y^3z^2$

$$, (-x - 3)x^2y^2z^2 + 2x^2yz^2(-xy - 3y), 2x^2y^2z(-xy - 3y)$$

). Compute the potential function for this field whose potential at the origin is -3.

. Calculate the value of the potential at the point $p=(5, -1, -9)$.

- 1) $-\frac{372531}{10}$ 2) $\frac{437319}{10}$ 3) 16197 4) $\frac{664077}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(7t+1)\sin(2t)(9\cos(4t)+10), (6t+4)\sin(t)(9\cos(4t)+10)\}$$

Indication: it is necessary to represent

the curve to check whether it has intersection points.

- 1) 54618.2 2) 13655. 3) 58031.8 4) 34136.6

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{xz^2 - 7xyz^2, 4x^2z^2, 6xy^2 - 9x^2y^2z\}$ and the surface

$$S \equiv \left(\frac{8+x}{5}\right)^2 + \left(\frac{y}{5}\right)^2 + \left(\frac{z}{3}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -3.91429×10^6 2) -954703 . 3) 2.19582×10^6 4) -2.5777×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 51

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-2yz - 3) \sin(xz) + z(-2xyz - 3x) \cos(xz)$, $-2xz \sin(xz) - 4y, x(-2xyz - 3x) \cos(xz) - 2xy \sin(xz)$.
). Compute the potential function for this field whose potential at the origin is 1.
 . Calculate the value of the potential at the point $p=(2,-4,5)$.

- 1) $-31 + 74 \sin[10]$ 2) $\frac{529}{5} + 74 \sin[10]$ 3) $\frac{637}{5} + 74 \sin[10]$ 4) $\frac{1033}{5} + 74 \sin[10]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (3 \cos(t) + 3) \left(\frac{(\sqrt{3}-1) \cos(t)}{2\sqrt{2}} - \frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} \right), \sin(2t) (3 \cos(t) + 3) \left(\frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} + \frac{(1+\sqrt{3})}{2} \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 10.6029 2) 4.60288 3) 9.60288 4) 5.60288

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \left\{ e^{-2y^2+z^2} - 6yz, -4y + \cos[x^2 + 2z^2], e^{x^2-2y^2} + 5z \right\}$ and the surface

$$S \equiv \left(\frac{5+x}{3} \right)^2 + \left(\frac{7+y}{1} \right)^2 + \left(\frac{-7+z}{3} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -84.4009 2) -43.7009 3) -32.6009 4) 37.6991

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 52

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = \left(\frac{z(3x - 3xyz)}{xz + 1} + (3 - 3yz) \log(xz + 1) - 2xy - 4x, -x^2 - 3xz \log(xz + 1), \frac{x(3x - 3xyz)}{xz + 1} - 3xy \log(xz + 1) \right)$

-). Compute the potential function for this field whose potential at the origin is -5.
- . Calculate the value of the potential at the point $p=(-2,-5,0)$.

1) $\frac{63}{10}$ 2) 7 3) $\frac{91}{5}$ 4) $-\frac{133}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (2\cos(t) + 4) \left(\frac{\cos(t)}{2} - \frac{1}{2}\sqrt{3}\sin(t) \right), \sin(2t) (2\cos(t) + 4) \left(\frac{\sin(t)}{2} + \frac{1}{2}\sqrt{3}\cos(t) \right) \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 12.7372 2) 18.3372 3) 14.1372 4) 15.5372

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \left\{ -1 + e^{2y^2}, -5xz - \sin[x^2 - 2z^2], -9 + 5yz + \cos[y^2] \right\}$ and the surface

$$S \equiv \left(\frac{6+x}{7} \right)^2 + \left(\frac{-9+y}{2} \right)^2 + \left(\frac{3+z}{2} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -10025.4 2) 13721.1 3) 5277.88 4) 4750.18

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 53

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-yz(x-xyz)\sin(xyz) + (1-yz)\cos(xyz) + 3, -xz(x-xyz)\sin(xyz) - xz\cos(xyz), -xy(x-xyz)\sin(xyz) - xy\cos(xyz))$. Compute the potential function for this field whose potential at the origin is -4. Calculate the value of the potential at the point $p=(3,5,9)$.

- 1) $549 - 132 \cos[135]$ 2) $-\frac{2423}{5} - 132 \cos[135]$ 3) $-\frac{247}{5} - 132 \cos[135]$ 4) $5 - 132 \cos[135]$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \frac{\left(\frac{\sqrt{3}}{2} - \frac{\sin(t)}{2}\right) \cos(t) (8 \cos(t) + 10)}{\sin^2(t) + 1}, \frac{\left(\frac{1}{2} \sqrt{3} \sin(t) + \frac{1}{2}\right) \cos(t) (8 \cos(t) + 10)}{\sin^2(t) + 1} \right\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 154.938 2) 16.3381 3) 170.338 4) 47.1381

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{4x + 6z + \sin[y^2 - 2z^2], 9xyz + \cos[z^2], e^{-2x^2+y^2} - 3y + 9z\}$ and the surface

$$S \equiv \left(\frac{2+x}{1} \right)^2 + \left(\frac{-8+y}{6} \right)^2 + \left(\frac{8+z}{4} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 9470.16 2) 15783.4 3) -41035.4 4) 78915.4

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 54

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = \left(\frac{y(-3xz-z)}{xy+1} - 3z \log(xy+1), \frac{x(-3xz-z)}{xy+1} + 3, (-3x-1) \log(xy+1) \right)$

-). Compute the potential function for this field whose potential at the origin is 0.
- . Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) 1.19118 2) -1.60882 3) 2.59118 4) 1.59118

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \dashrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(6t+8) \sin(2t) (\cos(15t) + 9), (5t+6) \sin(t)\}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

1) 5382. 2) 2990. 3) 4186. 4) 1794.

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-3y, -2y^2z + 5xy^2z^2, 8xyz^2\}$ and the surface

$$S \equiv \left(\frac{-4+x}{2} \right)^2 + \left(\frac{-2+y}{5} \right)^2 + \left(\frac{-8+z}{3} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) 1.09498×10^6 2) -1.40783×10^6 3) 782131. 4) 1.87711×10^6

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 55

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$$\begin{aligned} &z(2xz + yz) + 2xz^2 - 2, \\ &xz^2 + 4y, \\ &xz(2x + y) + x(2xz + yz) \end{aligned}$$

). Compute the potential function for this field whose potential at the origin is 1.

. Calculate the value of the potential at the point $p=(7,2,7)$.

- 1) $-\frac{5483}{2}$ 2) $-\frac{10966}{5}$ 3) 5483 4) $-\frac{49347}{10}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, 2\pi] \longrightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ -\frac{\cos(t)(4\cos(t)+7)}{\sin^2(t)+1}, -\frac{\sin(t)\cos(t)(4\cos(t)+7)}{\sin^2(t)+1} \right\}$$

Indication: it is necessary to represent
the curve to check whether it has intersection points.

- 1) 44.1345 2) 62.7345 3) 75.1345 4) 25.5345

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) =$

$$\left\{ e^{y^2+z^2} + 2yz, 7z + \sin[2x^2 + z^2], -9xy + \sin[x^2 + y^2] \right\}$$
 and the surface

$$S \equiv \left(\frac{-2+x}{7} \right)^2 + \left(\frac{-4+y}{2} \right)^2 + \left(\frac{1+z}{6} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 0. 2) -1.9 3) -1.5 4) -1.4

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 56

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (xy^2z^2(-e^{xyz}) - yz e^{xyz} - 6x + 3y, x^2yz^2(-e^{xyz}) - xz e^{xyz} + 3x, x^2y^2z(-e^{xyz}) - xy e^{xyz})$

). Compute the potential function for this field whose potential at the origin is 0.

. Calculate the value of the potential at the point $p=(3,1,-1)$.

$$1) -\frac{108}{5} + \frac{3}{e^3} \quad 2) -\frac{234}{5} + \frac{3}{e^3} \quad 3) \frac{207}{5} + \frac{3}{e^3} \quad 4) -18 + \frac{3}{e^3}$$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \left\{ \sin(2t) (5 \cos(t) + 8) \left(\frac{(1+\sqrt{3}) \cos(t)}{2\sqrt{2}} - \frac{(\sqrt{3}-1) \sin(t)}{2\sqrt{2}} \right), \sin(2t) (5 \cos(t) + 8) \left(\frac{(1+\sqrt{3}) \sin(t)}{2\sqrt{2}} + \frac{(\sqrt{3}-1) \cos(t)}{2\sqrt{2}} \right) \right\}$$

Indication: it is necessary to represent

the curve to check whether it has intersection points.

$$1) 90.083 \quad 2) 18.083 \quad 3) 60.083 \quad 4) 114.083$$

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{\cos[y^2+z^2], -2y - \sin[x^2-z^2], -2 - \sin[2x^2-2y^2]\}$ and the surface

$$S \equiv \left(\frac{-5+x}{6} \right)^2 + \left(\frac{3+y}{8} \right)^2 + \left(\frac{4+z}{6} \right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

$$1) -2412.74 \quad 2) -2895.34 \quad 3) 5550.16 \quad 4) -6273.54$$

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 57

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz(3yz+2)\cos(xy), 3z\sin(xy) + xz(3yz+2)\cos(xy) - 6y, 3y\sin(xy) + xy(3yz+2)\cos(xy))$,

1). Compute the potential function for this field whose potential at the origin is 6.

2). Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

1) 11.9066 2) 5.40662 3) -14.5934 4) 22.9066

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{ (4t+9)\sin(2t), (8\cos(2t)+9), (3t+1)\sin(t) \}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 1192.22 2) 265.424 3) 1324.62 4) 1854.22

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{4 - 7xz^2, -3y, 4xy^2z - 6x^2yz^2\}$ and the surface

$$S \equiv \left(\frac{6+x}{1}\right)^2 + \left(\frac{6+y}{4}\right)^2 + \left(\frac{z}{1}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) -71266.5 2) -36425.1 3) -15837. 4) 47511.

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 58

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-yz e^{xyz} - 4xy + 2y, -2x^2 - xz e^{xyz} + 2x, xy(-e^{xyz}))$.

Compute the potential function for this field whose potential at the origin is -2.

Calculate the value of the potential at the point $p=(-5,5,1)$.

$$1) -\frac{6488}{5} - \frac{1}{e^{25}} \quad 2) -301 - \frac{1}{e^{25}} \quad 3) -\frac{3921}{5} - \frac{1}{e^{25}} \quad 4) -\frac{4978}{5} - \frac{1}{e^{25}}$$

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r}: [0, \pi] \rightarrow \mathbb{R}^2$$

$$\mathbf{r}(t) = \{(9t+7) \sin(2t) (6 \cos(13t) + 8), (3t+7) \sin(t) (6 \cos(13t) + 8)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

$$1) 5556.65 \quad 2) 27779.8 \quad 3) 13890.3 \quad 4) 44447.2$$

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{9x^2 z^2 - 6yz^2, 9x^2 yz^2, -6x^2 z^2\}$ and the surface

$$S \equiv \left(\frac{-4+x}{5}\right)^2 + \left(\frac{2+y}{5}\right)^2 + \left(\frac{4+z}{8}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

$$1) 2.31127 \times 10^7 \quad 2) 7.00385 \times 10^6 \quad 3) 1.821 \times 10^7 \quad 4) 3.01165 \times 10^7$$

Further Mathematics - Grado en Ingeniería - 2023/2024

04-Line-surface integral-Test 1 for serial number: 59

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (yz(3yz - 3z)e^{xyz} - 6xy - 2y, -3x^2 + xz(3yz - 3z)e^{xyz} + 3ze^{xyz} - 2x, (3y - 3)e^{xyz} + xy(3yz - 3z)e^{xyz})$. Compute the potential function for this field whose potential at the origin is -2. Calculate the value of the potential at the point $p=(-5,7,3)$.

1) $-457 + \frac{54}{e^{105}}$ 2) $-\frac{457}{2} + \frac{54}{e^{105}}$ 3) $-\frac{5027}{10} + \frac{54}{e^{105}}$ 4) $\frac{914}{5} + \frac{54}{e^{105}}$

Exercise 2

Compute the area of the domain whose boundary is the curve

$r: [0, \pi] \rightarrow \mathbb{R}^2$
 $r(t) = \{(2t+8)\sin(2t)(5\cos(11t)+5), (7t+3)\sin(t)(5\cos(11t)+5)\}$

Indication: it is necessary to represent the curve to check whether it has intersection points.

1) 5572.97 2) 15125. 3) 11145. 4) 7960.97

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-9yz, -2xz, 2x^2z^2\}$ and the surface

$$S \equiv \left(\frac{2+x}{3}\right)^2 + \left(\frac{y}{6}\right)^2 + \left(\frac{9+z}{8}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

1) 50379.2 2) -125945. 3) -138540. 4) -62972.2

Further Mathematics - Grado en Ingeniería - 2023/2024 04-Line-surface integral-Test 1 for serial number: 60

Exercise 1

Consider the vectorial field $\mathbf{F}(x,y,z) = (-yz(-2yz-y)\sin(xyz) - 2y^2, -xz(-2yz-y)\sin(xyz) + (-2z-1)\cos(xyz) - 4xy, -xy(-2yz-y)\sin(xyz) - 2y\cos(xyz))$. Compute the potential function for this field whose potential at the origin is -3.

. Calculate the integral of the potential function ϕ over the domain $[0,1]^3$.

- 1) -12.2993 2) 14.7007 3) -4.29934 4) -7.79934

Exercise 2

Compute the area of the domain whose boundary is the curve

$$\mathbf{r} : [0, \pi] \longrightarrow \mathbb{R}^2 \\ \mathbf{r}(t) = \{(3t+9)\sin(2t)(\cos(18t)+5), (7t+3)\sin(t)(\cos(18t)+5)\}$$

Indication: it is necessary to represent the curve to check whether it has intersection points.

- 1) 670.378 2) 2680.38 3) 6700.38 4) 10050.4

Exercise 3

Consider the vectorial field $\mathbf{F}(x,y,z) = \{-7xy^2z^2, -x^2y + 3yz^2, 4y + 7y^2z\}$ and the surface

$$S \equiv \left(\frac{4+x}{1}\right)^2 + \left(\frac{8+y}{7}\right)^2 + \left(\frac{-8+z}{5}\right)^2 = 1$$

Compute $\int_S \mathbf{F} \cdot d\mathbf{S}$.

Indication: Use Stoke's Theorem if it is necessary.

- 1) 1.43019×10^7 2) -8.68328×10^6 3) -5.10781×10^6 4) -1.32803×10^7